

Neutrino Oscillations vs Charged-Lepton Oscillations

Question: Why don't we see $\mu \rightarrow e$ oscillations?

(Note: $\mu \rightarrow e$ oscillations would be very rapid due to their large Δm^2)

Neutrino Oscillations vs Charged-Lepton Oscillations

Question: Why don't we see $\mu \rightarrow e$ oscillations?

(Note: $\mu \rightarrow e$ oscillations would be very rapid due to their large Δm^2)

Answer: Neutrinos are identified by their flavors, while charge leptons are identified by their mass!

Neutrinos are identified by their flavor!

$$\begin{aligned} \nu_e &= \cos\theta \nu_1 + \sin\theta \nu_2 \\ \nu_\mu &= -\sin\theta \nu_1 + \cos\theta \nu_2 \end{aligned}$$

Useful!

$$\begin{aligned} \nu_1 &= \cos\theta \nu_e - \sin\theta \nu_\mu \\ \nu_2 &= \sin\theta \nu_e + \cos\theta \nu_\mu \end{aligned}$$

Not Useful!

When we measure neutrinos in oscillation experiments, we are insensitive to their mass; however, we are very sensitive to their flavor!

Charged Leptons are identified by their mass!

$$l_{\alpha} = \cos\theta l_1 + \sin\theta l_2$$

$$l_{\beta} = -\sin\theta l_1 + \cos\theta l_2$$

Not Useful!

$$e = l_1 = \cos\theta l_{\alpha} - \sin\theta l_{\beta}$$

$$\mu = l_2 = \sin\theta l_{\alpha} + \cos\theta l_{\beta}$$

Useful!

When we measure charged leptons, we are insensitive to their flavor; however, we are very sensitive to their mass!

Neutrinos Won't Oscillate if their Masses are Fixed!

Consider $\pi^+ \rightarrow \mu^+ \nu_\mu$

I. If the μ^+ is unmeasured $\Rightarrow \nu_\mu = -\sin\theta \nu_1 + \cos\theta \nu_2$

Neutrino Oscillations!

II. If the μ^+ is measured so precisely that the ν_μ mass is known \Rightarrow

$$\nu_2 = \sin\theta \nu_e + \cos\theta \nu_\mu$$

No Neutrino Oscillations!